

PSSA and Keystone Exams
Summer 2023 Workshops

Keystone Algebra 1

Baskets of Tomatoes

Handscoring
Training Set 2

Small baskets of tomatoes are sold at a vegetable stand for \$3 per basket. Large baskets of tomatoes are sold at the stand for \$5 per basket. Only whole numbers of baskets may be purchased.

A customer purchases a total of 8 baskets of tomatoes and pays \$36.

A. Write and solve a system of equations that models the number of small baskets (x) and the number of large baskets (y) that the customer purchases. Show or explain all your work.

The equation of 8 baskets totaling \$36 would be six \$5 baskets which equals \$30 and two \$3 baskets which equals 6. $\$30 + \$6 = \$36$ and $6 \text{ baskets} + 2 \text{ baskets} = 8 \text{ baskets}$

163 / 1000

Another customer claims that he can purchase a total of 10 baskets of tomatoes and pay \$45.

B. Use a system of equations that describes this other customer's purchase to explain why the claim is incorrect.

10b is supposed to be equal to \$45. There is supposed to be exactly 10 baskets that will equal exactly \$45.

107 / 1000

F

16. Small baskets of tomatoes are sold at a vegetable stand for \$3 per basket. Large baskets of tomatoes are sold at the stand for \$5 per basket. Only whole numbers of baskets may be purchased.

A customer purchases a total of 8 baskets of tomatoes and pays \$36.

- A. Write and solve a system of equations that models the number of small baskets (x) and the number of large baskets (y) that the customer purchases. Show or explain all your work.

small baskets
 xxxxx xxxxx xxxxx xxxxx xxxxx 24

large number
 yyy yyy yyy yyy 11

$$24 + 11 = 36$$

F

16. *Continued.* Please refer to the previous page for task explanation.

Another customer claims that he can purchase a total of 10 baskets of tomatoes and pay \$45.

- B. Use a system of equations that describes this other customer's purchase to explain why the claim is incorrect.

The whole purchase is \$5 to get a large baskets of tomatoes.

$$45 \times 5 = 50$$

He wouldn't have
enough money.

16. Small baskets of tomatoes are sold at a vegetable stand for \$3 per basket. Large baskets of tomatoes are sold at the stand for \$5 per basket. Only whole numbers of baskets may be purchased.

A customer purchases a total of 8 baskets of tomatoes and pays \$36.

- A. Write and solve a system of equations that models the number of small baskets (x) and the number of large baskets (y) that the customer purchases. Show or explain all your work.

$$3(x) + 5(y) = 36$$

$$3(2) + 5(6) = 36$$

2 small baskets
and 6 large
baskets

I did guess and check and
these two numbers worked out
perfect for this equation.

F

16. *Continued.* Please refer to the previous page for task explanation.

Another customer claims that he can purchase a total of 10 baskets of tomatoes and pay \$45.

- B. Use a system of equations that describes this other customer's purchase to explain why the claim is incorrect.

$$\begin{array}{l} 8x = 45 \\ 8(5) = 45 \end{array}$$

\$5 is the most money that a basket costs and you can only buy 8, and he wants 10. If you set the \$8 and \$5 it still doesn't work.

Small baskets of tomatoes are sold at a vegetable stand for \$3 per basket. Large baskets of tomatoes are sold at the stand for \$5 per basket. Only whole numbers of baskets may be purchased.

A customer purchases a total of 8 baskets of tomatoes and pays \$36.

A. Write and solve a system of equations that models the number of small baskets (x) and the number of large baskets (y) that the customer purchases. Show or explain all your work.

$x + y = 36$ The customer purchased 2 small baskets and 6 large baskets. 2 small baskets equals \$6 and 6 large baskets equal \$30 giving that customer their total of \$36.

166 / 1000

Another customer claims that he can purchase a total of 10 baskets of tomatoes and pay \$45.

B. Use a system of equations that describes this other customer's purchase to explain why the claim is incorrect.

$x + y = 45$

There is no arrangement of baskets to get a total of 10 baskets to equal \$45.

- The customer bought 2 small baskets and 6 large ones.

F

16. *Continued.* Please refer to the previous page for task explanation.

Another customer claims that he can purchase a total of 10 baskets of tomatoes and pay \$45.

- B. Use a system of equations that describes this other customer's purchase to explain why the claim is incorrect.

$$\begin{array}{l} 3x + 5y = 45 \\ 1x + 1y = 10 \end{array} \quad = \quad \begin{array}{l} x = 2.5 \\ y = 7.5 \end{array}$$

This customer is incorrect because in Part A it stated that ONLY whole numbers of baskets may be purchased.

16. Small baskets of tomatoes are sold at a vegetable stand for \$3 per basket. Large baskets of tomatoes are sold at the stand for \$5 per basket. Only whole numbers of baskets may be purchased.

A customer purchases a total of 8 baskets of tomatoes and pays \$36.

- A. Write and solve a system of equations that models the number of small baskets (x) and the number of large baskets (y) that the customer purchases. Show or explain all your work.

x = small baskets
 y = large baskets

$$\begin{aligned} 3x + 5y &= 36 \\ x + y &= 8 \end{aligned}$$

$$x + y = 8$$

$$x = 8 - y$$

$$3x + 5y = 36$$

$$3(8 - y) + 5y = 36$$

$$24 - 3y + 5y = 36$$

$$24 + 2y = 36$$

$$2y = 12$$

$$y = 6$$

$$x + y = 8$$

$$x + 6 = 8$$

$$x = 2$$

The customer bought 2 small baskets of tomatoes and 6 large baskets of tomatoes.

F

16. *Continued.* Please refer to the previous page for task explanation.

Another customer claims that he can purchase a total of 10 baskets of tomatoes and pay \$45.

- B. Use a system of equations that describes this other customer's purchase to explain why the claim is incorrect.

$$\begin{array}{rcl}
 x + y = 10 & x = 10 - y & x + 7.5 = 10 \\
 3x + 5y = 45 & 3(10 - y) + 5y = 45 & x = 2.5 \\
 & 30 - 3y + 5y = 45 & \\
 & 30 + 2y = 45 & \\
 & 2y = 15 & \\
 & y = 7.5 &
 \end{array}$$

This other customer's claim is incorrect because in order for it to be true, he would have had to buy 2.5 small baskets of tomatoes and 7.5 large baskets of tomatoes. However, this is not possible because only whole numbers of baskets may be purchased. As a result, this other customer's claim is incorrect.

16. Small baskets of tomatoes are sold at a vegetable stand for \$3 per basket. Large baskets of tomatoes are sold at the stand for \$5 per basket. Only whole numbers of baskets may be purchased.

A customer purchases a total of 8 baskets of tomatoes and pays \$36.

- A. Write and solve a system of equations that models the number of small baskets (x) and the number of large baskets (y) that the customer purchases. Show or explain all your work.

$$36 = 3x + 5y$$

$$8 = x + y \rightarrow 24 = 3x + 3y \quad 8 = x + y$$

$$12 = 2y$$

$$6 = y$$

$$2 = x$$

The customer can buy 6 large baskets of tomatoes and 2 small baskets.

F

16. *Continued.* Please refer to the previous page for task explanation.

Another customer claims that he can purchase a total of 10 baskets of tomatoes and pay \$45.

- B. Use a system of equations that describes this other customer's purchase to explain why the claim is incorrect.

$$45 = 3s + 5l$$

$$10 = s + l \rightarrow 30 = 3s + 3l$$

$$15 = 2l$$

$$7.5 = l$$

$$10 = s + 7.5$$

$$2.5 = s - 7.5$$

The system of equations does prove that the customer could have bought 7.5 large baskets and 2.5 small baskets, but only whole numbers of baskets may be purchased making that claim incorrect.

Small baskets of tomatoes are sold at a vegetable stand for \$3 per basket. Large baskets of tomatoes are sold at the stand for \$5 per basket. Only whole numbers of baskets may be purchased.

A customer purchases a total of 8 baskets of tomatoes and pays \$36.

A. Write and solve a system of equations that models the number of small baskets (x) and the number of large baskets (y) that the customer purchases. Show or explain all your work.

$$3x + 5y = 36$$

$$3x = 36$$

$$\div 3 \quad \div 3$$

$$x = 12$$

$$5y = 36$$

$$\div 5 \quad \div 5$$

$$y = 7.1$$

117 / 1000

Another customer claims that he can purchase a total of 10 baskets of tomatoes and pay \$45.

B. Use a system of equations that describes this other customer's purchase to explain why the claim is incorrect.

$$3x + 5y = 45$$

$$3x = 45$$

$$\div 3 \quad \div 3$$

$$x = 15$$

$$5y = 45$$

$$\div 5 \quad \div 5$$

$$y = 9$$

$$3(15) + 5(9) = 105$$

66 / 1000

F

16. Small baskets of tomatoes are sold at a vegetable stand for \$3 per basket. Large baskets of tomatoes are sold at the stand for \$5 per basket. Only whole numbers of baskets may be purchased.

A customer purchases a total of 8 baskets of tomatoes and pays \$36.

- A. Write and solve a system of equations that models the number of small baskets (x) and the number of large baskets (y) that the customer purchases. Show or explain all your work.

$$3x + 5y = 36$$

$$x + y = 8$$

$$y = 8 - x$$

$$3x + 5(8 - x) = 36$$

$$3x + 40 - 5x = 36$$

$$-2x = -4$$

$$x = 2$$

$$3(2) + 5y = 36$$

$$6 + 5y = 36$$

$$5y = 30$$

$$y = 6$$

2 small baskets and 6 large baskets were purchased. The customer's purchase equaled \$36 and $x=2$ and $y=6$. $x+y=8$ which is the total amount of baskets she purchased.

16. **Continued.** Please refer to the previous page for task explanation.

Another customer claims that he can purchase a total of 10 baskets of tomatoes and pay \$45.

- B. Use a system of equations that describes this other customer's purchase to explain why the claim is incorrect.

$$10 = x + y$$

$$45 = 3x + 5y$$

$$x = 10 - y$$

$$45 = 3(10 - y) + 5y$$

$$45 = 30 - 3y + 5y$$

$$45 = 30 + 2y$$

$$15 = 2y$$

$$7.5 = y$$

This is not correct because a customer can not take half a basket, only a whole.

Small baskets of tomatoes are sold at a vegetable stand for \$3 per basket. Large baskets of tomatoes are sold at the stand for \$5 per basket. Only whole numbers of baskets may be purchased.

A customer purchases a total of 8 baskets of tomatoes and pays \$36.

A. Write and solve a system of equations that models the number of small baskets (x) and the number of large baskets (y) that the customer purchases. Show or explain all your work.

$$\begin{array}{ll} 36 = 3x + 5y & x + y = 8 \\ 36 = 3(2) + 5(6) & (2) + (6) = 8 \\ 36 = 6 + 30 & 8 = 8 \\ 36 = 36 & x = 2, y = 6 \\ & (2, 6) \end{array}$$

The customer bought two small baskets, and six large baskets.

151 / 1000

Another customer claims that he can purchase a total of 10 baskets of tomatoes and pay \$45.

B. Use a system of equations that describes this other customer's purchase to explain why the claim is incorrect.

$45 = 3x + 5y$	$x + y = 10$	$45 = 3x + 5y$	$x + y = 10$
		As you can	
see this customer			
$45 = 3(5) + 5(9)$	$(5) + (9) = 10$	$45 = 3(5) + 5(15)$	$5 + 15 = 10$
is incorrect. No matter what			
$45 = 15 + 45$	$14 \text{ doesn't} = 10$	$45 = 15 + 75$	$20 \text{ doesn't} = 10$
numbers you put in for x and y			
$45 \text{ doesn't} = 60$		$45 \text{ doesn't} = 90$	
you will never be able to pay			
\$45 for any combination of 10			
baskets.			

983 / 1000

Keystone: Baskets of Tomatoes (Algebra 1), Training Set Two

Subject: Algebra 1

Item: Baskets of Tomatoes

Grade: HS

Name _____

Number	Score	Notes
T2-1		
T2-2		
T2-3		
T2-4		
T2-5		
T2-6		
T2-7		
T2-8		
T2-9		
T2-10		